Meeting C++ 2022

Keeping Track of Your Deadlines in Time-Critical Systems

Matthias Killat



Keeping Track of Your Deadlines in Time-Critical Systems

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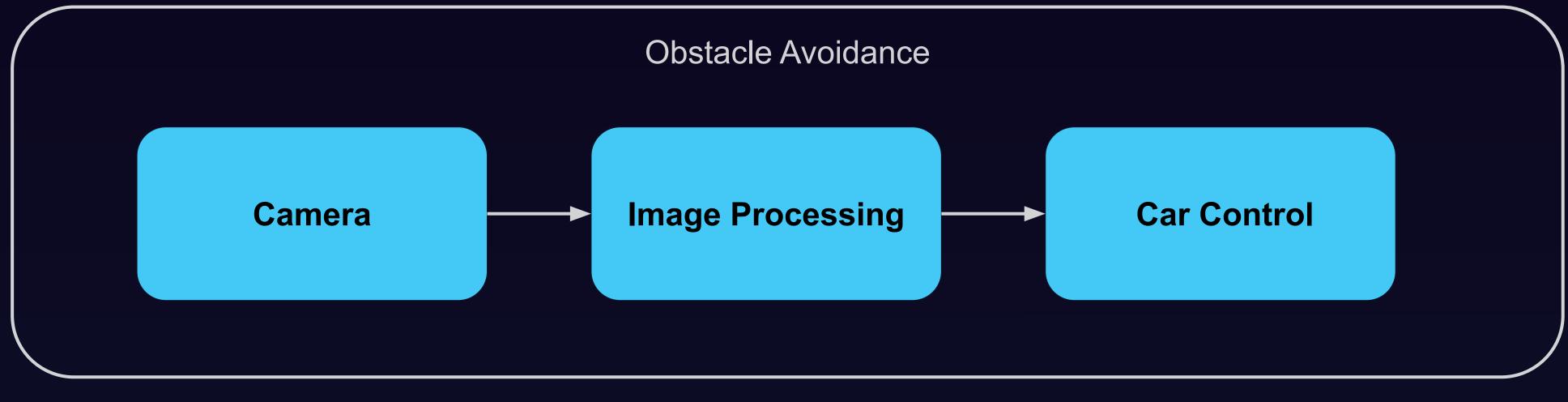
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Introduction

- Real-Time Systems
- Problem Statement
- Minimal Use Case



Time-Critical Systems



25 frames per second Dete

- Runs in a loop
- If we do not want to drop frames we need to process each frame in at most 40ms
- Deadlines like this are typical for many real word applications
- Modeled as real-time system

Incorrect results are useless Correct but late results are also useless...

Real-time correctness also depends on the time at which the results are available.

Detect obstacle

Braking or steering decision

s each frame in at most 40ms plications

Real-Time Systems

Deadline

- Time until some function must have completed
- Generally measured by wall-clock in practical applications

Real-Time System

- Impose deadlines on some functions
- Hard deadlines must be met or it is a system failure
- Soft deadlines failure to meet the deadline leads to degraded performance
- Often use multiple threads
- Requires OS with fair scheduling

Progress

- A function is said to make progress if it completes in finite time
- Deadlines are more strict: require progress within a concrete time span

Reasons for lack of progress

- Deadlock: programming error or partial system failure
- Starvation: scheduling or program logic error
- Priority inversion: special case of starvation

How Can We Ensure Deadlines Are Met?

- Gather requirements and identify deadlines
- 2. Separate real-time algorithms and protocols
- 3. Avoid certain problems like priority inversion
 - Limit data sharing between threads
 - Limit context switches
 - Avoid locks (lock-free programming)
 - Careful thread priority assignment \bigcirc

Problem: How can we guarantee that deadlines are met by our implementation?

Depends on:

- Hardware
- Operating system and scheduler configuration
- Algorithm inputs (worst case)
- Other processes running in parallel

Assume we want to build a Real-Time application in C++

It is generally impossible to check at compile time whether deadlines are met.

Minimal version

```
#include "monitoring.hpp"
```

```
using namespace std::chrono_literals;
```

EXPECT_PROGRESS_IN(100ms);

```
time_critical_function(x, y);
```

CONFIRM_PROGRESS;

Syntax

- Simple to include in a project (header only)
- Use compact std::chrono literal syntax
- Should look distinct (e.g. like macros)
- Function style only if they take arguments
- Look and feel like Google test expectations

Semantics

- EXPECT_PROGRESS_IN starts a deadline section
- CONFIRM_PROGRESS marks the end of the deadline
- Acts like parentheses
- Any code in the deadline section is monitored
- If the deadline is not met (wall-clock), a handler is invoked

Naming functions is hard ...

What about multi-threading?

```
#include "monitoring.hpp"
using namespace std::chrono_literals;
// thread not yet monitored
START_THIS_THREAD_MONITORING;
  no active deadline
EXPECT_PROGRESS_IN(100ms, 73);
// deadline ID 73 is active
time_critical_function(x, y);
// more monitored code
CONFIRM_PROGRESS;
// no active deadline
STOP_THIS_THREAD_MONITORING;
```

Support for multiple threads

- Toggle monitoring for individual threads
- Interface refers to the current thread that is executing this code section

Checkpoint IDs

- Refer to a deadline by some checkpoint ID
- IDs must be managed externally (no duplicate detection)
- Multiple threads can execute the same section.



How are deadline violations detected?

```
#include "monitoring.hpp"
using namespace std::chrono_literals;
// thread not yet monitored
START_THIS_THREAD_MONITORING;
// no active deadline
EXPECT_PROGRESS_IN(100ms, 73);
// deadline ID 73 is active
time_critical_function(x, y);
// more monitored code
CONFIRM_PROGRESS;
// no active deadline
STOP_THIS_THREAD_MONITORING;
```

```
Detection by the thread itself (Passive)
//pseudo code
//assume sufficiently accurate clock
auto timestamp = now();
EXPECT_PROGRESS_IN(100ms, 73)
  deadline_id = 73;
  start = now();
  deadline = start + 100ms;
CONFIRM_PROGRESS
  end = now();
  if(end > deadline)
    report_violation(deadline_id, end);
```

How are deadline violations detected?

```
#include "monitoring.hpp"
using namespace std::chrono_literals;
// thread not yet monitored
START_THIS_THREAD_MONITORING;
  no active deadline
EXPECT_PROGRESS_IN(100ms, 73);
// deadline ID 73 is active
time_critical_function(x, y);
// more monitored code
CONFIRM_PROGRESS;
// no active deadline
STOP_THIS_THREAD_MONITORING;
```

Challenges

- Where do we store the deadline for each thread?
- What type should the timestamp have?
- Timestamp overflow
- How do we compare timestamps?

What if the active thread does not make progress?

What if the thread does not make progress?

```
#include "monitoring.hpp"
using namespace std::chrono_literals;
// thread not yet monitored
START_THIS_THREAD_MONITORING;
  no active deadline
EXPECT_PROGRESS_IN(100ms, 73);
// deadline ID 73 is active
time_critical_function(x, y);
// more monitored code
CONFIRM_PROGRESS;
// no active deadline
STOP_THIS_THREAD_MONITORING;
```

Possible reasons for deadline violation

- Deadlock
- Starvation
- Deadline section takes unexpectedly long

The thread may never detect the violation or detect it too late.

Background monitoring thread

- Active monitoring (e.g. polling)
- High priority
- Low synchronization overhead

Interesting problem ...

How do we solve it efficiently?

Design

- Requirements and Constraints
- Performance Considerations
- System Overview



Functionality

- 1. Detect deadline violations in multiple threads
- 2. Ensure violations are detected even in the case of deadlocks
- 3. Track deadline locations using checkpoint IDs and source location
- 4. Allow setting a custom deadline handler
- 5. Disable the monitoring completely or run only in passive mode
- Optional mode to gather runtime statistics 6.

Usage

- Easy to integrate in existing C++ code
- No additional dependencies apart from STL

Requirements

// initialize and start active monitoring START_ACTIVE_MONITORING STOP_ACTIVE_MONITORING

monitoring of the current thread START_THIS_THREAD_MONITORING STOP_THIS_THREAD_MONITORING

establish a deadline EXPECT_PROGRESS_IN(time, id) CONFIRM_PROGRESS

//custom deadline handler SET_MONITORING_HANDLER(handler) UNSET_MONITORING_HANDLER



Performance Considerations

Performance

- Low influence on regular computation
- Minimal data sharing
- Lock-free happy path (no deadlines violated)
- Remaining lock contention should be low

Real-time safety

- Predictable response time with fair scheduling
- Avoid dynamic memory allocation
- No exceptions
- Avoid blocking unless required by design

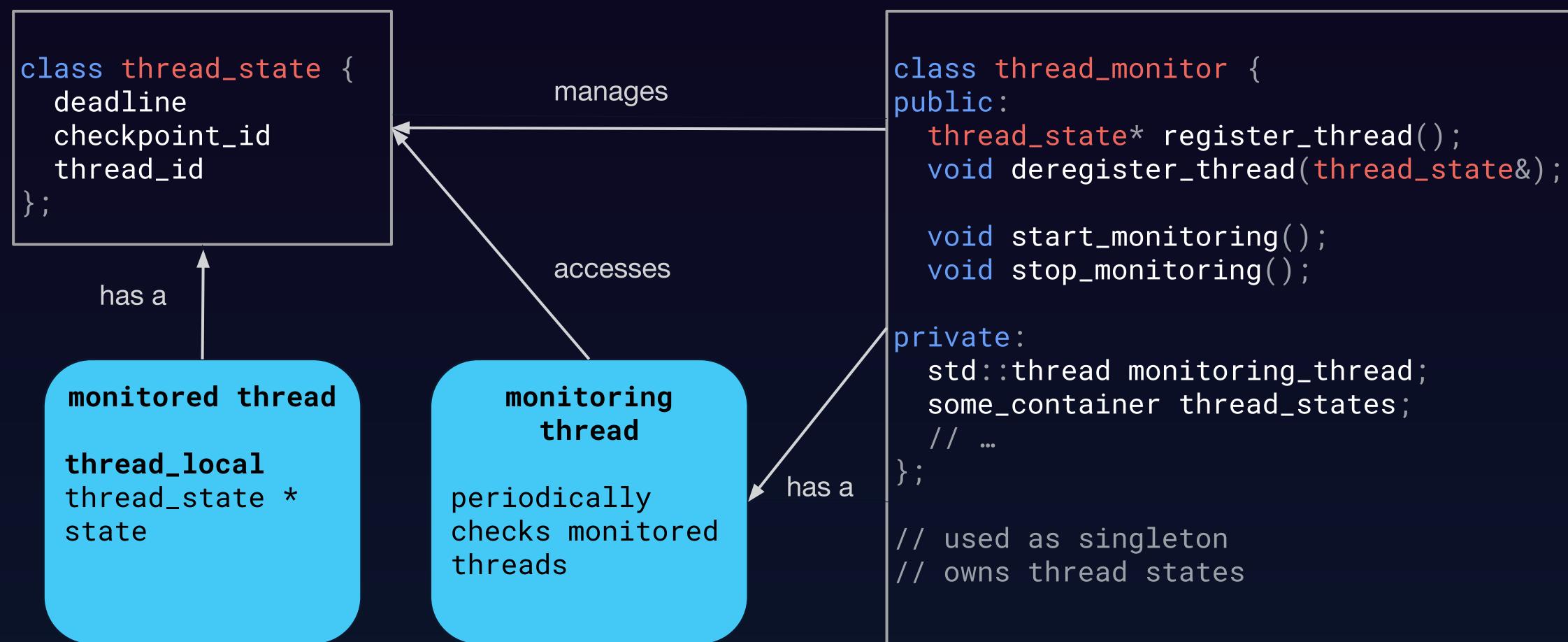
Performance has to be considered early in design.

- Limit the number of monitored threads
- Deadlines have an upper limit
- Fast detection can only be ensured if the background thread gets sufficient priority and time to run
- No nested deadlines (e.g. across function calls)

```
EXPECT_PROGRESS_IN(300ms);
f(x, y);
EXPECT_PROGRESS_IN(100ms);
g(x, z);
CONFIRM_PROGRESS;
CONFIRM_PROGRESS;
```

Advanced version supports nested deadlines.

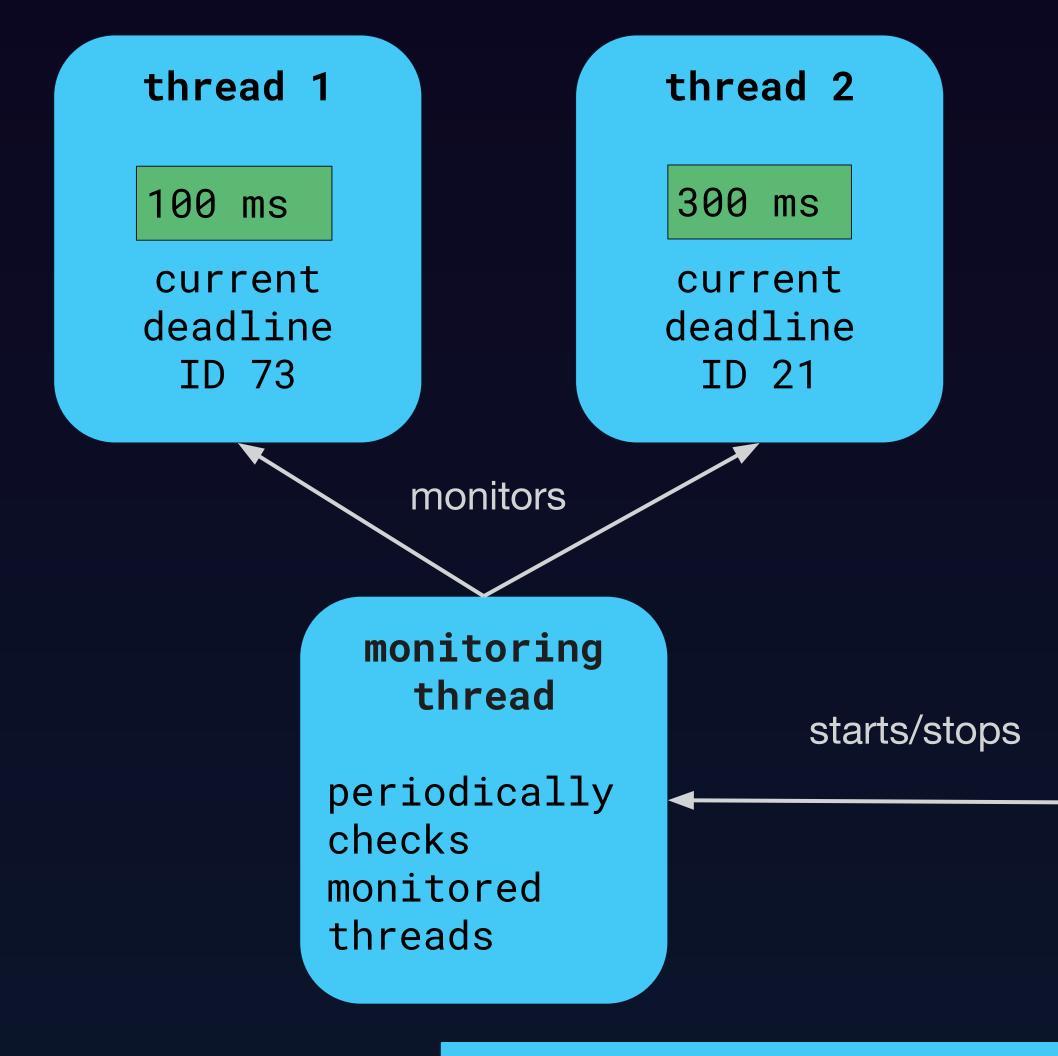
Restrictions



System Design



System Design



Almost no lock-based synchronization between threads

```
class thread_monitor {
public:
  thread_state* register_thread();
  void deregister_thread(thread_state&);
  void start_monitoring();
  void stop_monitoring();
private:
  std::thread monitoring_thread;
  some_container thread_states;
};
```

That could really work!

Onward to the ...

Implementation

- Checking Deadlines
- Measuring Time
- Nested Deadlines



Representing Deadlines

- Deadlines are time points
- Time points are durations measured relatively to some epoch
- Epoch is a fixed reference time like
 - \circ 1st of January, 1970) or
 - system start
- Durations are number of ticks in some time unit (e.g. nanoseconds)

Constraint

Representation should be small for atomic operations (e.g. 8 bytes)

Assume

- time_t = uint64_t
- Some function to get the current time: time_t now();
- Reasonable arithmetic
- Nanosecond ticks

We can represent ~293 years and do not care about time overflow for now.

Checking Deadlines

```
class thread_state {
  time_t deadline{0}
  id_t checkpoint_id{0}
  tid_t thread_id;
};
   properly initialized when thread
// is monitored
thread_local thread_state* ts;
EXPECT_PROGRESS_IN(time, id) :
ts \rightarrow deadline = now() + time;
ts->deadline_id = id;
```

- Consider a deadline of **0** as invalid for now
- Store deadline in a thread local state
- Afterwards the deadline is valid

Limit thread interaction by using thread local scope.

Checking Deadlines

```
CONFIRM_PROGRESS :
// invalidate deadline
auto d = ts->deadline.exchange(0);
if(is_valid(d) && is_violated(d) {
  report_violation(ts);
bool is_valid(time_t d) {
  return d != 0;
bool is_violated(time_t d) {
  return now() > d;
```

We have to invalidate violated deadlines to avoid multiple violation reports.



- Deadline might have been invalidated by background thread
- Atomic exchange prevents multiple reports

d

Monitoring Thread

- Can access the thread state of each thread
- Reads and checks the deadlines (periodically or when needed)
- Deadline check is lock-free (atomic read)
- Deadline violation invokes a CAS operation to reset the deadline (Why?)

Interaction of two monitored thread

Thread 1 vs. Thread 2	Register Thread	Unregister Thread	Expect	Confirm	Monitoring Thread Check
Register Thread	Mutex	Mutex	None	None	Mutex
Unregister Thread	Mutex	Mutex	None	None	Mutex
Expect	None	None	None	None	Lock-free
Confirm	None	None	None	None	Lock-free

- Mutex contention is rare only when monitoring of a thread starts or ends
- Lock-free interaction happens frequently
- Deadline reset via expensive CAS is also rare if deadline violation is rare

The happy path is lock-free.

Monitoring Thread

```
// check a thread deadline
void check_deadline(thread_state_t& ts) {
 auto d = ts->deadline.load();
 if(is_valid(d) && is_violated(d)) {
    // mark as reported
    if(ts->deadline.compare_exchange_strong
      (d, <mark>0</mark>)) {
      report_violation(ts);
  run periodically/if needed in a thread
void check_threads() {
  for(auto &ts : registered_thread_states) {
    check_deadline(ts);
```

- Atomic deadline reset is required
- Requires CAS
 - After the thread loads d the deadline could be reset by the monitored thread
- Ensures not missing deadline violations
- Single report per violation

Monitoring thread runs periodically

- Could run on notification only but this requires notification
- Condition variables are relatively expensive
- No priority queue

Deadline Monitoring Example

Possible interleaving

Time (in ms)	Thread 1	Thread 2	Deadlines	Monitoring Thread (20ms)	Violation
0	EXPECT(15ms, 1)		d1(15)	Check nothing	
	f(x)		d1		
20		EXPECT(50ms, 2)	d1,d2(70)	Check d1, d2	d1(+5)
		g(y)	d1, d2		
40	CONFIRM		d2	Check d2	d1(+25)
			d2		
60		CONFIRM		Check d2	
70	EXPECT(15ms, 1)		d1(90)		
	f(x)		d1	Check d1	
90	CONFIRM				d1(+5)
				Check nothing	

If the monitoring thread is scheduled on time, each deadline violation will be detected with a predictable delay.

Generalizations

1. Overflow Tolerance 2. Nested Deadlines

Measuring Time

```
#include <chrono>
using time_t = uint64_t;
using clock_t = chrono::steady_clock;
using time_unit_t = chrono::nanoseconds;

time_t now() {
  auto tp = chrono::time_point_cast<time_unit_t>(clock_t::now());
  // usually signed int64_t representation
  auto ticks = tp.time_since_epoch().count();
  return static_cast<time_t>(ticks);
}
```

Bad

- Loses chrono unit safety, but is only used internally
- Generally not safe in the overflow case
 - o Depends on clock_t::now()
 - o Depends on rep_t count();
- Usually rep_t is signed

Good

- Monotonic clock
- Not exposed to user; API can use chrono::literals
- Unsigned overflow is well-defined (modular arithmetics)

Overflow Tolerance

Advantages

- Epoch does not matter
- System can run forever
- Can use smaller types than $time_t = uint64_t$ (e.g. only for milliseconds)
 - Can use some arbitrary real-time counter
 - Can use the extra bits for additional information

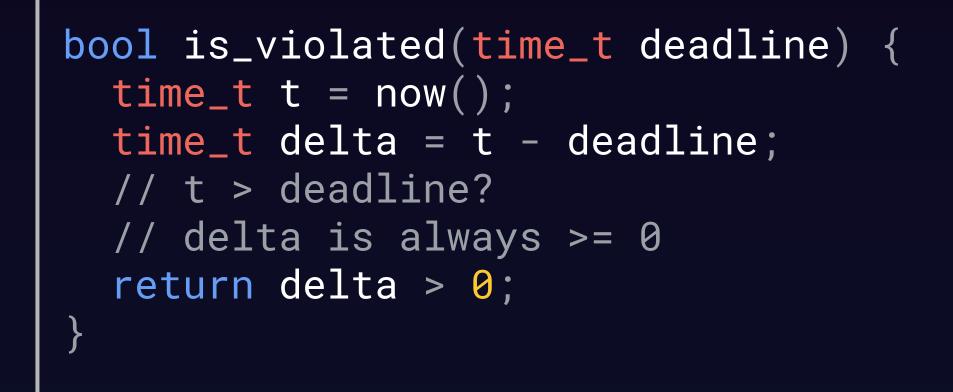
Disadvantages

- Clock must support overflow
- Slightly more complex violation checks
- Deadline invalidation becomes more complex

Time can be considered as a cycle with power of two length.

Measuring Time Intervals

Wrong - does not handle overflow correctly



Correctly handles overflow

```
using stime_t = int64_t;
bool is_violated(time_t deadline) {
  time_t t = now();
  time_t delta = t - deadline;
  stime_t s = static_cast<stime_t>(delta)
  return s > 0;
```

Problem

Need to check whether the current time t precedes the deadline on a cycle of length $M = 2^{64}$

- Modular arithmetic wrt. M
- Time points ahead of t by at most M/2 are considered to be later
- Other half cycle is considered before

Observation

Due to two's complement these are equivalent

- 1. deadline is before t (violation)
- 2. 0 < delta < M/2
- 3. The most significant bit of delta is 0
- 4. The signed representation of delta is >0

Is Overflow only a Theoretical Problem?

That depends on

- Resolution of the clock
- Epoch of the clock (how close do we start to overflow?)
- Application runtime
- Safety requirements (proof that overflow is never a problem)

With nanosecond ticks and epoch being system start we can count for ~293 years with signed 64 bit integers.

Why do we have to be careful with chrono::steady_clock?

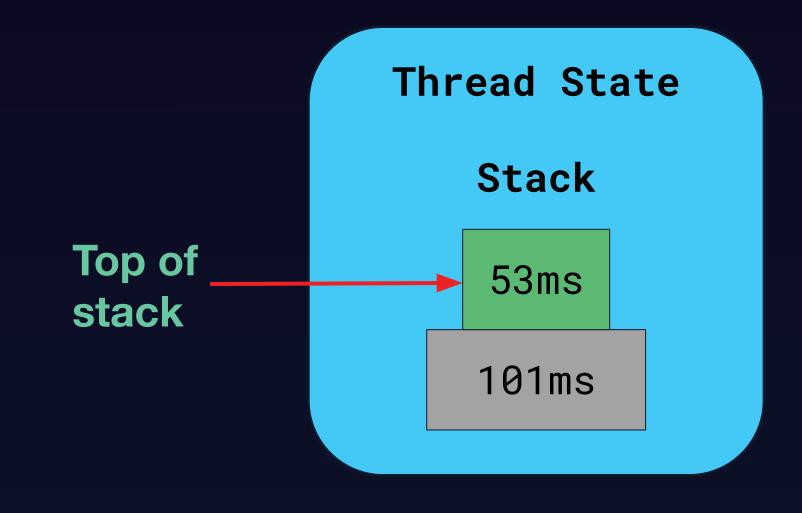
- Signed integer overflow is undefined behavior
- It does not define the epoch (usually system start, but we cannot rely on that)
- The representation type of the ticks can be signed count() will return a signed or unsigned type depending on implementation (usually signed)

Overflow problems can be avoided with access to a monotonic clock with unsigned time ticks.

Nested Deadlines

- Important since functions declaring the deadlines may call each other
- Same idea, but now each thread keeps a stack of deadlines
- Nested deadlines are assumed to be monotonic for optimal detection (but do not need to be)

```
EXPECT_PROGRESS_IN(100ms, 1);
// time critical code
// maybe in another function
EXPECT_PROGRESS_IN(50ms, 2);
// more time critical code
CONFIRM_PROGRESS;
CONFIRM_PROGRESS;
```



Nested Deadlines - Stack

Properties

- 1. Lock-free
- 2. Single producer/consumer multiple readers
- 3. Monitored thread is producer and consumer
 - push/pop elements (deadlines)
- 4. Monitoring thread needs to
 - Read elements
 - Write elements (only to invalidate deadlines)
- 5. Stack elements must be trivially copyable

Stack memory management

- Intrusive stack elements, i.e. they expose internal node structure (next pointer)
- No or limited dynamic allocation

Skip implementation details

Nested Deadlines - Confirm



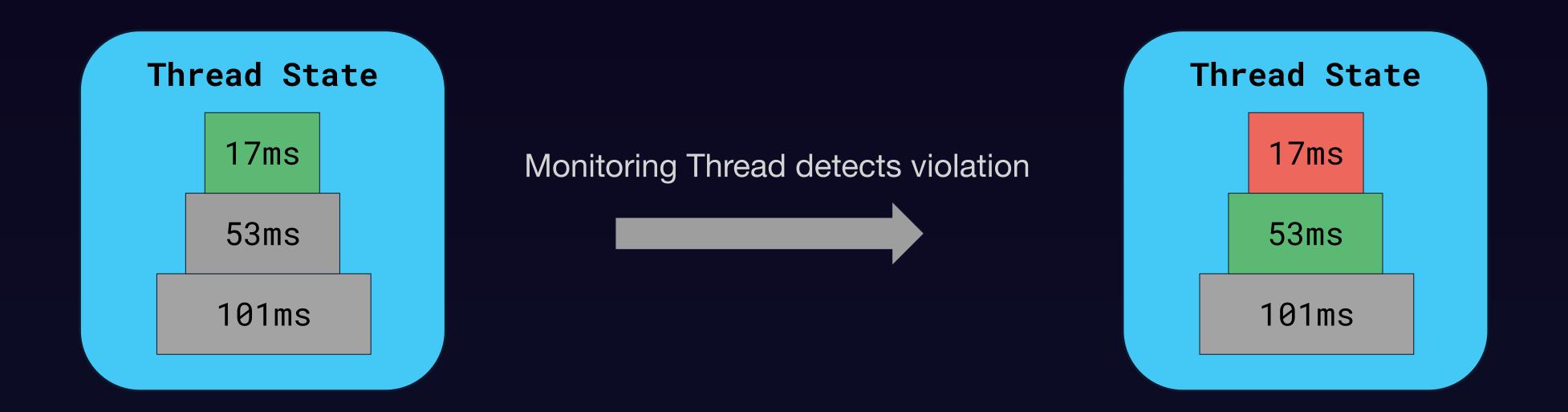
Monitoring thread will only check top of stack

- Sufficient for monotonic deadlines
- Delayed detection if not monotonic

No violation or violation detected by thread itself

- 1. Pop deadline from stack
- 2. If the deadline was not marked as invalidated by the monitoring thread check the deadline
- 3. Report violation if any

Nested Deadlines - Violation



Monitoring thread detected violation at top of stack

- 1. Invalidate top of stack deadline (no pop!)
- 2. Report violation
- 3. Check deadlines further down the stack from now on
 - Violated deadlines are invalidated

Time for some field tests.

Application

- Application Monitoring
- Timing Tests
- Runtime Statistics
- Performance



Monitoring Application Progress at Runtime

Cyclic time-critical application

```
#include "monitoring_api.hpp"
mutex g_mutex;
atomic<bool> g_run{true};
void thread_main() {
  // can reduce this boilerplate
  START_THIS_THREAD_MONITORING;
  SET_MONITORING_HANDLER(handler);
  while(g_run) {
    EXPECT_PROGRESS_IN(10ms, SOME_ID);
    lock_guard<mutex> guard(g_mutex);
    time_critical_function();
    CONFIRM_PROGRESS;
  STOP_THIS_THREAD_MONITORING;
```

Macro API advantages

- Source location
- Distinct from regular functions by convention
- Look and feel like e.g. Google Test
- Easy to disable

Possible API additions

Progress scope guard

- Reduces the risk of forgetting the closing CONFIRM_PROGRESS
- Restricts deadline end to scope end

Monitored thread

• Reduces thread monitoring boilerplate

```
#include "monitoring_api.hpp"
atomic<bool> g_deadline_violation{false};
// assumed to be set in general setup code
void handler(checkpoint &) {
  g_deadline_violation = true;
TEST_F(SomeFixture, deadline) {
  // test specific setup
  EXPECT_PROGRESS_IN(10ms, TEST_ID);
  int result = sut.critical_function();
  CONFIRM_PROGRESS;
  EXPECT_FALSE(g_deadline_violation);
  EXPECT_EQ(result, 73);
```

Timing Tests

Timing tests are problematic

- Threads may not be scheduled
- Timing expectation may be unreasonable for slower hardware
- Running under test conditions may be different from real conditions

Complements Google Test Framework

- Easy to add by just including a header
- Code to start monitoring in setup code
- Similar syntax for expected behavior

Combine to reduce boilerplate CONFIRM_PROGRESS EXPECT_FALSE(g_deadline_violation);

Runtime Statistics

For each time-critical section we can incrementally update

- Number of executions
- Number of violations
- Minimum and maximum runtime
- Mean runtime
- Standard deviation
- •

Overhead

- 1. Manage the statistics in e.g. (thread local) map<id_t,statistics>
- 2. Store the start time of a section
- 3. Compute statistics incrementally at the end of a section
- Update statistics 4.

Disabled by default due to overhead Can be further optimized!

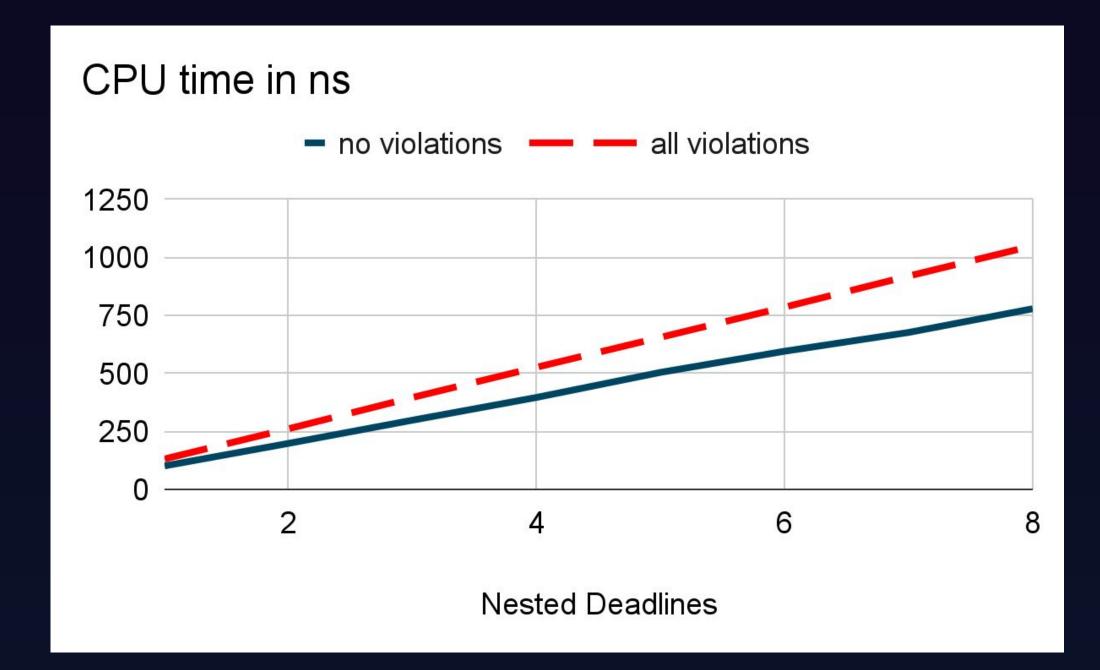
Example Output

deadline id 1 (10000us) count : 2000 violations: 0 min: 1635 max : 8427 mean : 5097.02 standard deviation : 988.378

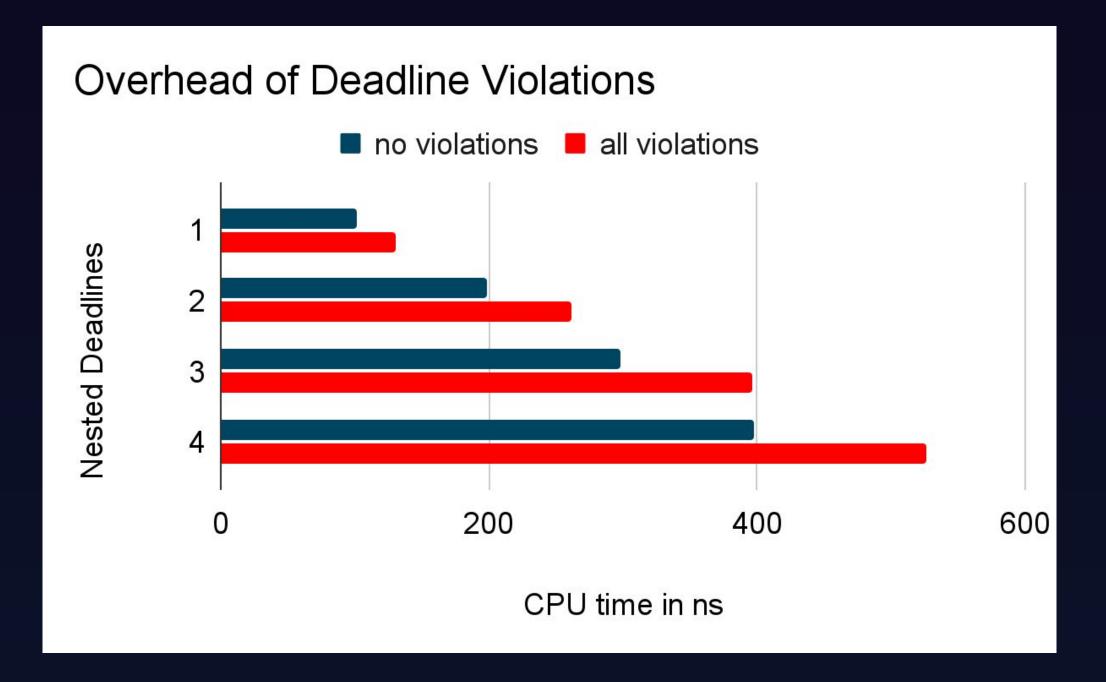
deadline id 2 (10000us) count : 1000 violations: 11 min: 1155 max: 10165 mean : 5646.78 standard deviation : 2587.96

Performance

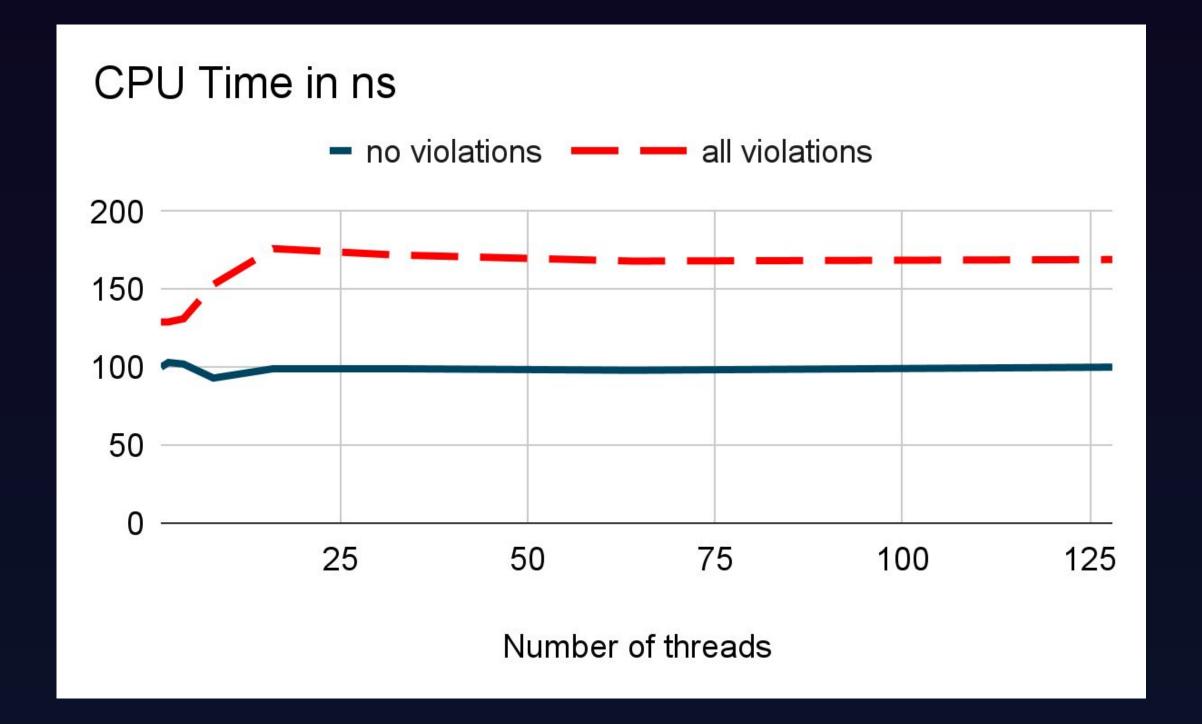
Google benchmark on Intel Core i7 x86-64 - 12 cores with gcc -O3 Measure CPU time of EXPECT_PROGRESS - CONFIRM_PROGRESS cycles without extra work



- Linear scaling wrt. number of nested deadlines
- Overhead per deadline is about 100ns (uncontended mutex lock unlock takes about 12ns)
- Deadline violations require ~1.3 times the CPU time (trivial handler that only sets a flag, no output)



Measure CPU time of EXPECT_PROGRESS - CONFIRM_PROGRESS cycles in multiple concurrent threads



- Monitored threads are independent from each other
- Limited lock-free data sharing has the intended effect
- Deadline violations appear to cause some minimal contention

Caution - Microbenchmarks often run with favorable cache conditions.

Performance

Features

- Visibly specify deadlines in code
 - The code is the source of truth
 - Can be matched with timing requirements in design
- Deadline violation will be detected eventually with fair scheduling
- Low detection delay (depends on configuration)
- Low overhead
- Monitoring can be disabled at compile time (no overhead)
- Measures statistics to e.g. fine tune deadlines on a specific system

Conclusion

We have implemented Framework to monitor deadlines in C++ that can easily be integrated into applications.

1. Data sharing

- Avoid if possible (e.g. thread local)
- If it cannot be avoided, keep the critical sections small
- Lock-free code can boost performance
- Blocking is ok for rare operations
- Measure the scaling with multiple threads

2. Time measurement

- Measuring time correctly is tricky
- Use a monotonic clock since we measure time intervals (stopwatch)
- With unsigned time stamps, the system can tolerate overflow and run forever
- Can use a real-time counter if available

3. Use Custom Data Structures and Memory allocation

- Reduce allocation at runtime (fragmentation, time overhead)
- Prefer preallocation \bigcirc
- Consider special purpose intrusive data structures

Key Takeaways

1. No interprocess monitoring

- Monitoring thread per process
- Can be extended by using efficient shared memory data transfer
 - Monitoring process instead of thread
 - Could use e.g. iceoryx zero-copy middleware to share deadline data

2. Inefficient monitoring thread

- Intentional time-based checking (performance)
- No mutex for synchronization of e.g. a priority queue
- No wake-up notification by other threads (for performance)
- Does not affect other threads until the system is overloaded

3. Inefficient statistics mode

- Simple test implementation uses a mutex and avoidable data sharing
- Only supposed to be used for development purpose

4. Not completely real-time safe yet

- Some data structures still use dynamic memory and exceptions
- Can be replaced with fixed size alternatives

Limitations

- Current Implementation: https://github.com/MatthiasKillat/progress_monitoring/
- Real-time counter: https://luckyresistor.me/2019/07/10/real-time-counter-and-integer-overflow/
- Lock-free buffer: Meeting C++ 2021, Lock-free Programming for Real-Time Systems
- Concurrency benchmarks: CppCon 2016, The Speed of Concurrency (is lock-free faster?), Fedor Pikus
- C++ Concurrency in Action, Anthony Williams
- Google Test: <u>https://github.com/google/googletest</u>
- iceoryx zero-copy middleware: <u>https://github.com/eclipse-iceoryx/iceoryx</u>
 - Real-time safe fixed size data structures
 - Lock-free data structures
 - Potentially useful for efficient monitoring across process boundaries \bigcirc

Suggestions for improvements are welcome!

References

The implementation is work in progress.

Could you spot it?

There is a subtle problem in the implementation related to invalid deadline representation.

Thanks for your Attention



Deadline Invalidation

- Generally 3 can be a valid deadline (especially if overflow is possible)
- Cannot invalidate by setting to Θ (by exchange or CAS)

Solution 1: Use least significant bit

- 1 becomes the invalid value
- Unsigned range is reduced by half
- Caution with monotonic counters, times are now represented by even values

Solution 2: Dual Counter - Use additional deadline validation value v

- Deadline d is valid if and only if d equals v
- Invalidation sets these to unequal (+1 or -1)
- Keep full unsigned range
- Caution with ABA problem
 - Requires correct invalidation scheme
 - Monotonic time is effectively an ABA counter

Both solutions increase the overhead slightly

Lock-free deadline stack

```
struct stack_entry {
    atomic<time_t> deadline; // payload
    stack_entry* next; // intrusive data
};
class deadline_stack {
public:
  void push(stack_entry&);
  stack_entry* pop();
  stack_entry* top();
  uint64_t generation();
private:
  atomic<stack_entry*> m_top{nullptr};
  // generation count
  atomic<uint64_t> m_generation{0};
```

Deadline Stack

- Allocation of entries happens externally
- In practice can be a simple thread local allocator
- stack_entry can be copied by memcpy
- 1. Lock-free push and pop are simple since there is only one thread modifying the stack
- 2. Each operation increases the generation counter
- 3. Counter has to synchronize data properly



Lock-free deadline stack

```
struct stack_entry {
    atomic<time_t> deadline; // payload
    stack_entry* next; // intrusive data
};
class deadline_stack {
public:
  void push(stack_entry&);
  stack_entry* pop();
  stack_entry* top();
  uint64_t generation();
private:
  atomic<stack_entry*> m_top{nullptr};
  // generation count
  atomic<uint64_t> m_generation{0};
```

Deadline Stack

```
Reading the stack concurrently
deadline_stack stack;
auto gen = stack.generation();
while(gen % 2 == 1) {
  // odd generation, write in progress
  // retry or give up
// sync with fence (gen read happens before)
auto *top = stack.top();
if(top)
  // read from top and traverse stack
  // cannot crash(!), even if stack changes
  if(gen == stack.generation()) {
    // read is valid (modulo ABA problem)
```

Measuring Time Intervals - Example

Why does this work?

```
using stime_t = int64_t;
bool is_violated(time_t deadline) {
  time_t t = now();
  time_t delta = t - deadline;
  stime_t s = static_cast<stime_t>(delta)
  return s > 0;
}
```

```
Assume we only use 8 bit counters, i.e.
time_t = uint8_t, stime_t = int8_t
```

```
EXPECT_PROGRESS_IN(10ns, 1)
```

```
• t0 = 250
```

• deadline = $250 + 10 = 4 \pmod{256}$

No overflow, not expired t = 253delta = 253 - 4 = 249s = -7 is < 0

Overflow, not expired t = 2 delta = 2 - 4 = 254s = -2 is < 0

Overflow, expired t = 5 delta = 5 - 4 = 1 s = 1 is > 0

What about t = 249? Expired, also OK!

Measuring Time Intervals - Correctness

Why does this work?

```
using stime_t = int64_t;
bool is_violated(time_t deadline) {
  time_t t = now();
  time_t delta = t - deadline;
  stime_t s = static_cast<stime_t>(delta)
  return s > 0;
}
```

- Modular arithmetic wrt. $M = 2^k$
- EXPECT_PROGRESS_IN(r, 1)
- \bullet r < M/2 = m
- Start time t0
- Deadline d = t0 + r

Case 1: deadline not yet violated

- m < delta <= M(since r<m)
- MSB of delta is 1
- s <= 0
- return false

Case 2: deadline violated by at most m

- 0 < delta < m
- MSB of delta is 0
- s > 0
- return true

Case 3: deadline violated by more than m

- 0 <= delta <= M (potential wraparound)
- MSB of delta is 0 or 1
- Cannot distinguish by using s
- Possibly incorrect result

Must check sufficiently often to avoid case 3 (with nanoseconds we have ~293 years)